

BIOSTATISTICS



- **STATISTICS** : is the science of compiling, classifying and tabulating numerical data & expressing the results in a mathematical or graphical form.
- **BIostatISTICS** : is that branch of statistics concerned with mathematical facts & data related to biological events.



MEASURES OF CENTRAL TENDENCY



- A single estimate of a series of data that summarizes the data - *the measure of central tendency.*
- **Objective:**
- To condense the entire mass of data.
- To facilitate comparison.



PROPERTIES



- Should be easy to understand and compute.
- Should be based on each and every item in the series.
- Should not be affected by extreme observations.
- Should be capable of further statistical computations.
- Should have sampling stability.





- The most common measures of central tendency that are used in dental sciences are :
 - ✓ **Arithmetic mean** – mathematical estimate.
 - ✓ **Median** – positional estimate.
 - ✓ **Mode** – based on frequency.



Arithmetic mean



- Simplest measure of central tendency.

- **Ungrouped data:**

✓ Mean =
$$\frac{\text{Sum of all the observations in the data}}{\text{Number of observations in the data}}$$

- **Grouped data:**

✓ Mean =
$$\frac{\text{Sum of all the variables multiplied by the corresponding frequency in the data}}{\text{Total frequency}}$$



MEDIAN:-



- ***Middle value in a distribution such that one half of the units in the distribution have a value smaller than or equal to the median and one half have a value greater than or equal to the median.***
- All the observations are arranged in the order of the magnitude.
- Middle value is selected as the median.
- Odd number of observations : $(n+1)/2$.
- Even number of observations: mean of the middle two values is taken as the mean.



MODE



- *The mode or the modal value is that value in a series of observations that occurs with the greatest frequency.*
- When mode is ill defined, it can be calculated using the relation
- ✓ **Mode = 3 median – 2 mean**





- Most commonly used: arithmetic mean.
- Extreme values in the series : median.
- To know the value that has high influence in the series: mode.



Measures of dispersion



- Dispersion is the **degree of spread or variation of the variable about a central value.**
- **Measures of dispersion used:**
- To determine the reliability of an average.
- To serve as basis for control of variability.
- To compare two or more series in relation to their variability.
- Facilitate further statistical analysis.



RANGE



- It is the simplest method, Defined as the difference between the value of the smallest item and the value of the largest item.
- This measure gives no information about the values that lie between the extremes values.
- Subject to fluctuations from sample to sample.



MEAN DEVIATION



- It is the average of the deviations from the arithmetic mean.
- **M.D = $\frac{\sum X - Xi}{n}$** , where Σ (**sigma**) is the sum of, **X** is the arithmetic mean, **X_i** is the value of each observation in the data, **n** is the number of observation in the data.



STANDARD DEVIATION(SD)



- Most important and widely used.
- Also known as root mean square deviation, because it is the square root of the mean of the squared deviations from the arithmetic mean.
- Greater the standard deviation, greater will be the magnitude of dispersion from the mean.
- A small SD means a higher degree of uniformity of the observations.



CALCULATION



- **For ungrouped data:**
- Calculate the mean(\bar{X}) of the series.
- Take the deviations (d) of the items from the mean by : $d = X_i - \bar{X}$, where X_i is the value of each observation.
- Square the deviations (d^2) and obtain the total ($\sum d^2$)
- Divide the $\sum d^2$ by the total number of observations i.e., $(n-1)$ and obtain the square root. This gives the standard deviation.
- Symbolically, standard deviation is given by:

$$SD = \sqrt{\sum d^2 / (n-1)}$$





▪ For grouped data with single units for class intervals:

▪ $S = \sqrt{\sum (X_i - X) \times f_i / (N - 1)}$

▪ Where,

- ✓ X_i is the individual observation in the class interval
- ✓ f_i is the corresponding frequency
- ✓ X is the mean
- ✓ N is the total of all frequencies





- For grouped data with a range for the class interval:

$$S = \sqrt{\sum (X_i - X) \times f_i / (N - 1)}$$

Where,

X_i is the midpoint of the class interval

f_i is the corresponding frequency

X is the mean

N is the total of all frequencies



COEFFICIENT OF VARIATION(C.V.)



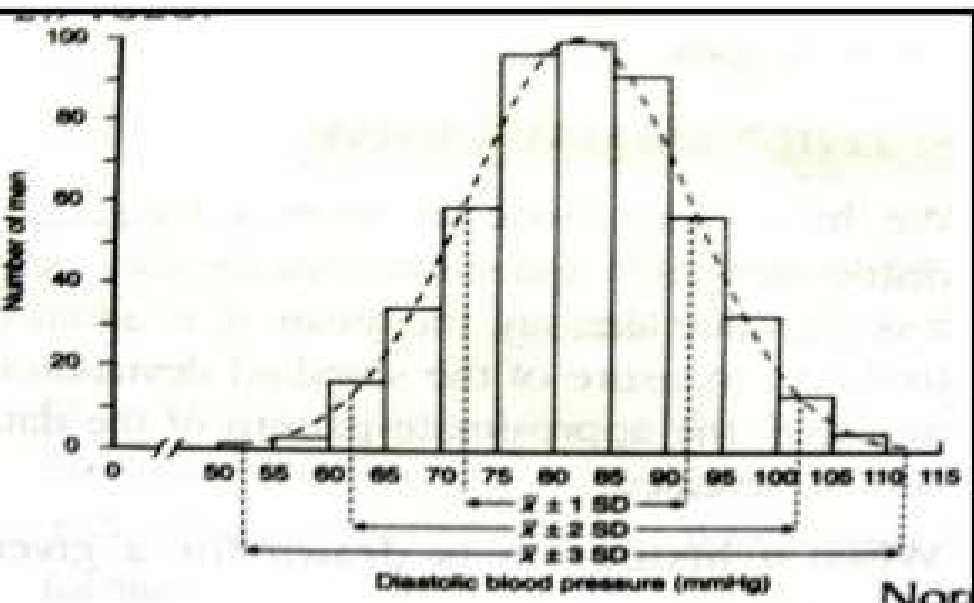
- A relative measure of dispersion.
- To compare two or more series of data with either different units of measurement or marked difference in mean.
- **$C.V.= (S \times 100) / X$**
- Where, C.V. is the coefficient of variation
- S is the standard deviation
- X is the mean
- Higher the C.V. greater is the variation in the series of data



NORMAL DISTRIBUTION CURVE

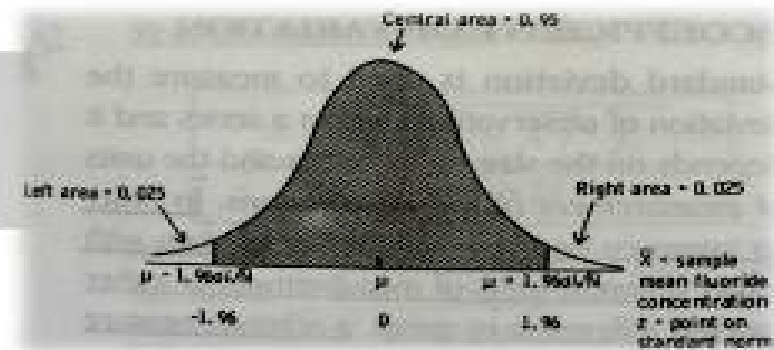


- Gaussian curve
- Half of the observations lie above and half below the mean
 - Normal or Gaussian distribution





Properties



- Bell shaped.
- Symmetrical about the midpoint.
- Total area of the curve is 1. Its mean zero & standard deviation 1.
- Height of curve is maximum at the mean and all three measures of central tendency coincide.
- Maximum number of observations is at the value of the variable corresponding to the mean, numbers of observations gradually decreases on either side with few observations at extreme points.





- Area under the curve between any two points can be found out in terms of a relationship between the mean and the standard deviation as follows:
 - ✓ Mean \pm 1 SD covers 68.3% of the observations
 - ✓ Mean \pm 2 SD covers 95.4% of the observations
 - ✓ Mean \pm 3 SD covers 99.7% of the observations
- These limits on either side of mean are called confidence limits.
- Forms the basis for various tests of significance .

